# Retinal image preprocessing, enhancement, and registration

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# 1 Introduction

The first fundus images were acquired after the invention of the ophthalmoscope. The concept of storing and analyzing retinal images for diagnostic purposes exists ever since. The first work on retinal image processing was based on analog images and regarded the detection of vessels in fundus images with fluorescein [1]. The fluorescent agent enhances the appearance of vessels in the image, facilitating their detection and measurement by the medical professional or the computer. However, fluorescein angiography is an invasive and time-consuming procedure and is associated with the cost of the fluorescent agent and its administration.

Digital imaging and digital image processing have proliferated the use of retinal image analysis in screening and diagnosis. The ability to accurately analyze fundus images has promoted the use of noninvasive, fundus imaging in these domains. Moreover, the invention of new imaging modalities, such as optical coherence tomography (OCT) and scanning laser ophthalmoscopy (SLO), has broadened the scope and applications of retinal image processing. This review regards both fundus imaging, as implemented by fundus photography and SLO and OCT imaging.

Retinal image analysis supports pertinent diagnostic procedures. A number of symptoms and diseases are diagnosed through observation of the human retina. Retinal image analysis is useful not only in the diagnosis of ophthalmic diseases, but also in that of systemic chronic diseases. Hypertension and diabetes are two important examples of such diseases that affect small vessels and microcirculation and which are noninvasively screened and assessed through the contribution of retinal image analysis [2, 3]. In this context, two widely employed tasks are the detection and measurement of anatomical features and properties, such as lesion detection and measurement of vessel diameters. Achieving these tasks typically includes a preprocessing stage, tuned according to the measured features and the method of image analysis. This preprocessing stage usually regards the normalization of image

intensities after image formation, as well as the enhancement of the image through noise reduction and contrast enhancement.

Image analysis methods capable of matching and aligning retinal images of the same eye have enabled the task of retinal image registration (RIR), which also plays a significant role in the diagnosis and the monitoring of diseases. By registering images acquired during the same examination, higher resolution and definition images of the retina can be obtained and enable high-precision measurements. Moreover, the registering images into mosaics facilitates mapping wider retinal regions than a single image does. Registration of images from different examinations facilitates follow-up examinations and assessment of treatment through the speed of symptom reversal.

# 2 Intensity normalization

Intensity normalization is the form of preprocessing closest to image acquisition, as it deals with the interpretation of pixel values for image formation. Digital sensors have built-in intensity normalization algorithms that subsequent image processing methods account for. Intensity normalization is also employed in the compensation of artifacts, due to uneven illumination of retinal tissue by the imaging modality.

# 2.1 Fundus imaging

The interplay between optics, light source, and eye shape casts illumination of the retina to be spatially uneven. This complicates feature detection and segmentation, often requiring local adaptation of processing.

Contrast normalization is usually applied to the "green" channel [4–7], as it is less sensitive to noise. Contrast enhancement in all three channels was proposed through 3D histogram equalization [8], or independent normalization of each channel [9]. In Ref. [10], intensity is adjusted based on information from the histograms of both red and green channels, in an attempt to reap benefits from information in both channels.

Generic, global approaches to intensity normalization have not fully solved this problem. Zero-mean normalization and unit variance normalization compensate only partially for lighting variation, as they introduce artifacts due to noise amplification [11-13]. A polynomial remapping of intensities [7] exhibits similar issues.

Generic, local approaches, based on the statistics of image neighborhoods, have been more effective and more widely adopted. To this end, Zhao et al. [14] employ a color-constancy method. Locally adaptive histogram equalization (CLAHE) [15] is one of the most widely used contrast normalization steps [16–23] including also adaptations of the initial method [24–26].

Retinal imaging-specific approaches estimate a model of illumination and rectify intensities according to the luminance it predicts [27–30]. This model is a mask image, where pixel values are estimates of tissue reflectivity. As the illumination source is usually unknown, this estimate is obtained assuming that local illumination variation is smaller than across the entire image.

# 2.2 Tomographic imaging

In OCT imaging, the need for intensity rectification stems from the automatic intensity rescaling and averaging of the sensor, which may differ in each scan. Generic intensity normalization has been applied to individual scans [31]. However, prominent noise reduction methods utilize multiple scans that image the same area and average measurements corresponding to the same tissue points [32–34]. The central step in such approaches is the registration of scans (see Section 4.2).

# 3 Noise reduction and contrast enhancement

Noise reduction and contrast enhancement are typical preprocessing steps in multiple domains of image analysis. Their goal is to improve image definition and fidelity, by accenting image structure and reducing image noise. Generic approaches to these tasks have been employed for all retinal image types. Nonetheless, approaches targeted to the particular modality and the subsequent analysis have been more widely adopted. Notably, in OCT imaging, noise reduction methods address an imaging artifact pertinent only to this modality, besides conventional image noise.

## 3.1 Fundus imaging

Generic approaches to local contrast and structural adjustment have been proposed [6,7,35–37], but are culpable in amplifying noise or noninteresting structures. Single-scale [38] and multi-scale [13, 39–41] linear filterings have also been tools of similar approaches but conversely they filter out useful fine image structure at fine scales. Morphological transformations have also been proposed, such as the contourlet [42] and the top-hat transformations [43], and were combined with histogram equalization [44] and matched filters [45]. Nonlinear filtering approaches have also been proposed. A diffusion-based "shock" filter was employed in Ref. [46]. In Ref. [47], inverse diffusion provided feature-preserving noise reduction. In Ref. [48], sparse coding and a representation dictionary were utilized to represent vessels and reconstruct the original image without noise.

Target-oriented contrast enhancement methods have also been tailored. Image sharpness was amplified by compensating for the blur of the eye's point spread function, through the modeling of the former [49]. Multi-orientation filtering kernels that mimic and highly correlate with vessel intensity profiles were used in Refs. [50–52] to enhance vessels. By modeling vessel appearance as ridge structures, the "vesselness," or Frangi filter in Ref. [53] has been widely utilized to accent vessels over the rest of the image.

Combination of multiple images has also been based on the information redundancy that is provided when imaging the same tissue multiple times, using averaging [54], or blind deconvolution [55]. The central step in these approaches is image registration (see Section 4.2).

# 3.2 Tomographic imaging

In OCT imaging, noise reduction addresses an additional source of noise, besides conventional noise due to electronics. "Speckle noise" is an OCT artifact [56], due to the reflective nature of the retina. So-called "speckles" are due to the interference of the illumination with back-scattered light.

Generic, single-image noise reduction has been based on linear filtering [57], adaptive transforms [58], wavelets [59–63], and wave atom transformations [64]. Nonlinear filtering has also been proposed, using conventional [65] or multiscale anisotropic diffusion [66]. Other approaches include regularization [67], PCA [68], Bayesian inference [69], and stochastic methods [70]. Compressive sensing and sparse representations were proposed in Refs. [71–73]. A comparative evaluation of such approaches can be found in Ref. [74].

Nevertheless, the main focus of noise reduction approaches is on speckle noise reduction, as speckles significantly obscure retinal structure in the acquired images. The majority of noise reduction approaches averages multiple, uncorrelated scans of the same section. In this way, image structure due to transient speckle noise is attenuated over structure due to actual tissue. Some techniques include adaptations upon the conventional OCT apparatus, leading to more complex image acquisition. In these cases, acquisition of uncorrelated scans is based on modulation of the incidence angle of illumination [75–77], detection angle of back-scattered light [77], laser illumination frequency [78–80], and illumination polarization [81–83]. On the other hand, spatial compounding techniques [32-34, 84] do not require modification of the OCT scanner, as they use the purposeful motion of the scanner to acquire overlapping and adjacent scans. Motion is a priori known minus the uncertainty of mechanical motion and, thus, only minor alignment is required. As the aforementioned techniques image the same tissue multiple times, they are limited by eye motion (i.e., saccadic). Thereby, the brevity of acquisition time is required to reduce the probability of corresponding motion artifacts.

Accidental and purposeful motions call for scan alignment, through image registration (see Section 4.2). Once scans are registered, postprocessing further enhances the volumetric signal. In Refs. [32, 85], 3D wavelet filters are applied to volumetrically registered scans. In Ref. [86], volumetric neighborhoods are matched and averaged. In Ref. [87], a physical model of speckle formation is employed and estimated as a convex optimization problem upon the volumetric data.

# 4 Retinal image registration

The problem of image registration regards a test and a reference image. The goal is the estimation of the aligning transformation that warps the test image, so that retinal points in the warped image occur at the same pixel locations as in the reference image. RIR is challenging due to optical differences across modalities or devices, optical distortions due to the eye lens and vitreous humor, anatomical changes due to lesions or disease, as well as acquisition artifacts. Viewpoint differences (i.e., due to eye motion) complicate image registration further, due to projective distortion of the curved surface of the eye.

Applications of RIR can be classified according to whether images are acquired in the same or different examinations. Images from the same examination are devoid of anatomic changes. If their overlap is significant, they can be combined into images of higher resolution and definition [88–90], enabling more accurate measurements. Images with small overlap are utilized to create image mosaics that broaden the sensor's field of view [91–93] (see Fig. 1).

Longitudinal studies of the retina [97, 98] are facilitated by the registration of images acquired at different examinations (i.e., initial and follow-up). Pertinent studies enable disease monitoring and treatment evaluation, through tracking of symptom reversal. In this context, accurate registration of images of the same retinal region proves valuable in the detection of minute but critical changes, such as local hemorrhages or differences in vasculature width (see Fig. 2).



110. 1

Registration of retinal images into a mosaic. *Top*: Original images, from the public dataset in Refs. [94, 95]. *Bottom*: Registration result, using Hernandez-Matas [96]. *From C. Hernandez-Matas, Retinal Image Registration Through 3D Eye Modelling and Pose Estimation (Ph.D. thesis), University of Crete, 2017.* 



#### FIG. 2

Registration of fundus images from the same retinal region that exhibit differences, for longitudinal studies. *Left*: Original images from the public dataset in Refs. [99, 100]. *Right*: Registration results using Hernandez-Matas [96].

From C. Hernandez-Matas, Retinal Image Registration Through 3D Eye Modelling and Pose Estimation (Ph.D. thesis), University of Crete, 2017.

### 4.1 Fundus imaging

Initial approaches to RIR attempted similarity matching of the entire test and reference image as encoded in the spatial [101–106] or frequency [107] domains. A central assumption in global methods is that intensities in the test and reference image are consistent. However, this does not always hold due to uneven illumination, eye curvature, and anatomical changes that may occur between the acquisition of the test and reference images.

Instead of matching all image pixels, local approaches rely on matching well-localized features or keypoints [90, 92, 98, 103, 108–131] (see Fig. 3). The approaches in Refs. [117, 123] match feature points, based only on their topology. General purpose features associated with local descriptors have been more widely utilized for RIR. SIFT [132] features are the ones that have provided the greatest accuracy [109, 130], with SURF [133] features comprising a close second [126, 128]. Harris corners associated with a descriptor of their neighborhood have also been proposed [120, 126]. Features tuned to retinal structures include vessels, bifurcations, and crossovers [92, 114, 115]. As these features are not associated with descriptors, SIFT or SURF descriptors have been computed at their locations to



#### FIG. 3

Corresponding features in two pairs of retinal images, from the public dataset in Ref. [99, 100]. *White dots* show matched features.

From C. Hernandez-Matas, Retinal Image Registration Through 3D Eye Modelling and Pose Estimation (Ph.D. thesis), University of Crete, 2017.

facilitate matching [134]. In general, local methods have been more widely utilized, particularly for images with small overlap, due to the increased specificity that point matches provide. Moreover, local methods are more suitable for the registration of images with anatomical changes, as they are robust to partial image differences. In addition, they require less processing power, leading to faster registration.

At the heart of local approaches is the establishment of point correspondences, or matches, across the test and reference images. Pertinent methods utilize these correspondences to estimate a transform that, optimally, brings the matched points into coincidence. As some correspondences are spurious, robust estimation of the transform is utilized to relieve the result from their influence [90].

A range of 2D and 3D transforms has been utilized. Similarity transforms include rotation, scaling, translation, and modulation of aspectratio [102-107, 110, 113, 114, 117, 119, 120, 124, 126, 127], while the affine transform is utilized to approximate projective distortion [92, 98, 101, 104, 110, 112–117, 117–120, 123–127, 131]. Projective transformations treat more appropriately perspective distortion at the cost of more degrees of freedom that imply higher computational cost and potential instability in optimization [90, 109, 110, 112, 128–130]. Quadratic transformations [92, 92, 104, 110, 111, 113, 114, 117, 119–122, 125, 125–127] allow further compensation for eye curvature. However, these transformations do not necessarily include consideration of the shape of the eye. Conversely, utilizing an eye model safeguards for unreasonable parameter model estimates and provides more accurate registration. In Refs. [96, 128–130], the RIR problem is formulated as a 3D pose estimation problem, solved by estimating the rigid transformation that relates the views from which the two images were acquired. Considering the problem in 3D enables 3D measurements, devoid of perspective distortion. Though 3D models account for perspective, they require knowledge of the shape of the imaged surface, either via modeling or via reconstruction. Even simple eye shape models have shown to improve registration accuracy of retinal images [128].

## 4.2 Tomographic imaging

Approaches to the registration of OCT images differ to fundus image registration approaches, due to their tomographic content. In some cases, OCT image registration is guided by the use of an additional fundus as a reference, which does not contain motion artifacts as it is instantaneously acquired.

Noise reduction in OCT images is based on averaging registered scans. In Ref. [32], the known translational motion of the scanner is assumed as accurate enough to juxtapose individual scans as volumetric data. In Ref. [33], an initial manual registration is refined through cross-correlation alignment. In Ref. [85], detecting the retinal pigment epithelium and requiring its continuity in adjacent scans provide a cue to registration. The work in Ref. [34] utilizes correlation maps of adjacent images. In Ref. [135], hierarchical affine-motion estimation approach is proposed. Low-rank and sparse image decomposition alignment has been employed in Ref. [136].

Eye motion estimation through OCT image registration has also been used to compensate for eye motion. In Ref. [137], an SLO-based eye tracker measured eye motion during image acquisition and images were registered according to these motion estimates. In Ref. [138], individual scans are registered to an SLO image. In Ref. [139], scans are registered without the use of a reference image; a particle filtering optimization is utilized to align scans in 3D as a dynamic system, which is optimization-based, but further exploits the temporal ordering of the scans and external information on their spatial arrangement. In Ref. [141], a semiautomatic approach is proposed to register and compare OCT scans, in order to study retinal changes in the corresponding data.

Mosaics of OCT volumes have been formed, using a fundus image as a reference. In Ref. [142], volumes are registered using vessel ridges and cross-correlation as a registration cue and based on the Iterative Closest Point algorithm. In Ref. [143], a reference image is not required, but adjacent volumes are registered based on a B-spline free-deformation method. In Ref. [144], a six-degree-of-freedom registration scheme for OCT volumes is proposed, which includes bundle adjustment corrections. In Refs. [145, 146], OCT volumes are registered in 3D without any prior knowledge of sensor or eye motion, based on correspondence of feature points.

#### 4.3 Intramodal vs. cross-modal image registration

The combination of imaging modalities results in improved understanding of the retinal tissue and its pathologies. Cross-modal registration enables analysis and comparison of images that may emphasize complementary retinal features. In tomographic imaging, registration of axial scans to a frontal, fundus image enables registration of OCT scans, despite eye motion (see Section 4.2).

MethodsinRefs.[112,115,116,131]registerfundusimages and fluoroangiographies, by performing vessel segmentation and matching common vessel structures across the two cross-modal images. Vessel segmentation, detection, and matching of bifurcation points have been utilized to establish point correspondences across cross-modal images [113, 121]. Keypoint features, such as SIFT and SURF, and their descriptors have also been employed for the same purpose [92, 109, 114, 116, 117, 119, 120]. In addition, novel descriptors associated with conventional keypoints have been proposed [125, 125, 131].

In Refs. [101, 102], mutual information was proposed as a cue to the registration of fundus and SLO images. The methods in Refs. [138, 142] register frontal OCT scans with SLO images, in a similar fashion. As frontal images are visually similar across modalities, registration is achieved by conventional matching of vessels or vessel features.

More challenging is the registration of axial OCT scans with frontal fundus images. This registration facilitates the acquisition of a volumetric reconstruction of retinal tissue, below the retinal surface. The works in Refs. [147–149] utilize retinal vessels as the cue to the registration of frontal fundus images and axial OCT scans, requiring vessel segmentation as an initial step. However, as retinal vessel segmentation is still an open problem, vessel segmentation errors are propagated in the registration phase. In Ref. [150], a feature-based approach is proposed, which capitalizes on corner features as control points and utilizes histograms of oriented gradients to better match the neighborhoods of these points. A robust approach is also included to remove correspondence outliers and estimate the transform that better registers the OCT scans to the fundus image.

# **5** Conclusions

A wide range of methods exists for the preprocessing, enhancement, and registration of retinal images acquired by conventional and emerging imaging modalities.

The preprocessing and enhancement tasks are required in a broad variety of uses. The most straightforward is the inspection of the image by the medical professional, where preprocessing and enhancement are required to preserve the fidelity of the acquired image while clarifying or accenting its structure and anatomical features. Preprocessing and enhancement are also utilized as initial steps in algorithmic image analysis, to facilitate and increase the accuracy of detection, recognition, and measurement of anatomical features. For these cases, generic image preprocessing methods have been applied, though more recently, approaches carefully select and tailor image preprocessing according to the subsequent image analysis goals. Due to the aforementioned variety of uses, benchmarking of image preprocessing tasks has been difficult and scarce. In addition, as preprocessing is typically only part of an image analysis method, when evaluation is available it regards the entire method and not the image preprocessing part in isolation.

RIR is also the basis for a wide spectrum of tasks. First, registration of multiple images allows to combine them into improved or wider retinal images. Moreover, RIR has been employed the comparison of retinal images, which is essential for monitoring a disease and the assessment of its treatment. As image registration is a well-defined task, attempts to provide pertinent benchmarks are starting to appear, as in Ref. [99] where existing datasets for RIR are compared and a benchmark methodology is also proposed. Still, there is a clear need for new approaches to benchmarking that will allow for more direct comparisons of methods and will account for optical phenomena, such as optical distortions due to the eye lens, vitreous humor, and chromatic aberrations.

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